



HARVARD  
Extension School

# CSCI E-74

## Virtual and Augmented Reality for Simulation and Gaming

*Fall term 2017*

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*Lesson 4 – Basic Architecture Implementation*



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# Automatic Vectors Normalization

Enable the automatic normalization

```
void glEnable(GL_NORMALIZE);
```

If enabled, normal vectors are normalized to unit length after transformation and before lighting.

This method is generally less efficient than `GL_RESCALE_NORMAL`.

See `glNormal` and `glNormalPointer`.



# Shade Model

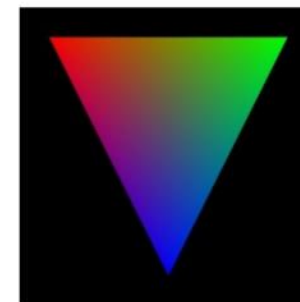
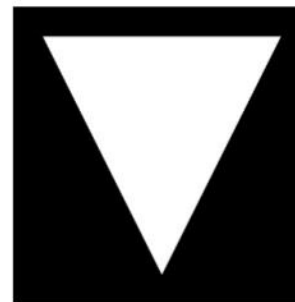
Selects the shading mode

```
void glShadeModel(GLenum mode);
```

mode Specifies a symbolic value representing a shading technique. Accepted values are GL\_FLAT and GL\_SMOOTH. The initial value is GL\_SMOOTH.

## Simplest Fragment Shading

- Flat color shading
  - `glShadeModel(GL_FLAT)`
- Interpolated color shading
  - `glShadeModel(GL_SMOOTH)`





# Rasterization Mode

select a polygon rasterization mode

```
void glPolygonMode(GLenum face, GLenum mode);
```

`face` Specifies the polygons that mode applies to. Must be `GL_FRONT_AND_BACK` for front- and back-facing polygons.

`mode` Specifies how polygons will be rasterized. Accepted values are `GL_POINT`, `GL_LINE`, and `GL_FILL`. The initial value is `GL_FILL` for both front- and back-facing polygons.

# Trigonometry Notes

## Trigonometric functions in C

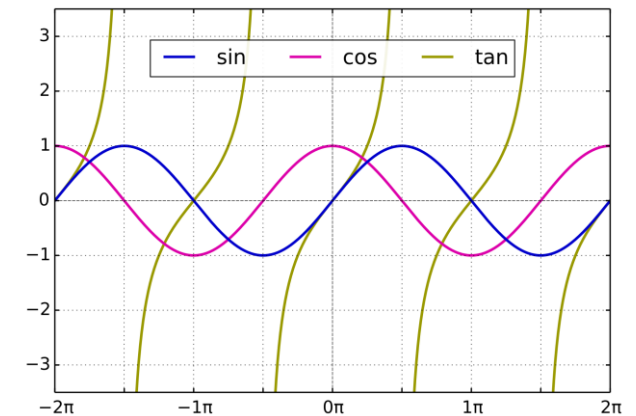
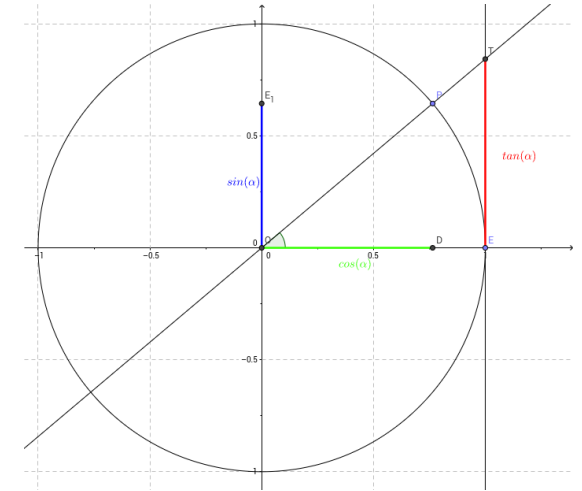
```
float sin(float angle);
float cos(float angle);
float tan(float angle);
float asin(float d);
float acos(float d);
float atan(float d);
```

Angle is expressed in radians!

**Degrees**  
{Conversion} = {Chart}

Degrees	Radians	Degrees	Radians
0°	0	210°	7 π/6
30°	π/6	225°	5 π/4
45°	π/4	240°	4 π/3
60°	π/3	270°	3 π/2
90°	π/2	300°	5 π/3
120°	2 π/3	315°	7 π/4
135°	3 π/4	330°	11 π/6
150°	5 π/6	360°	2 π
180°	π		

www.SwiftTips.com





# Trigonometry Notes

Degree to Radians

$$1^\circ = \pi/180^\circ = 0.005555556\pi = 0.01745329252 \text{ rad}$$

Then AR=AD\* 0.01745329252

Example

```
#define D2R 0.0174532925199432957692369076848
```

```
A = sin(angle*D2R);
```

Degrees

{Conversion} = {Chart}

Degrees	Radians	Degrees	Radians
0°	0	210°	7 π/6
30°	π/6	225°	5 π/4
45°	π/4	240°	4 π/3
60°	π/3	270°	3 π/2
90°	π/2	300°	5 π/3
120°	2 π/3	315°	7 π/4
135°	3 π/4	330°	11 π/6
150°	5 π/6	360°	2 π
180°	π		

www.SwifTips.com



# Trigonometry Notes

Radians to Degrees

$$1 \text{ rad} = 180^\circ/\pi = 57.295779513^\circ$$

Then  $AD=AR * 57.295779513^\circ$

Example

```
#define R2D 57.295779513082320876798154817014
```

```
angle = asin(1) *R2D;
```

Degrees

{Conversion} = {Chart}

Degrees	Radians	Degrees	Radians
0°	0	210°	7 π/6
30°	π/6	225°	5 π/4
45°	π/4	240°	4 π/3
60°	π/3	270°	3 π/2
90°	π/2	300°	5 π/3
120°	2 π/3	315°	7 π/4
135°	3 π/4	330°	11 π/6
150°	5 π/6	360°	2 π
180°	π		

www.SwiftTips.com

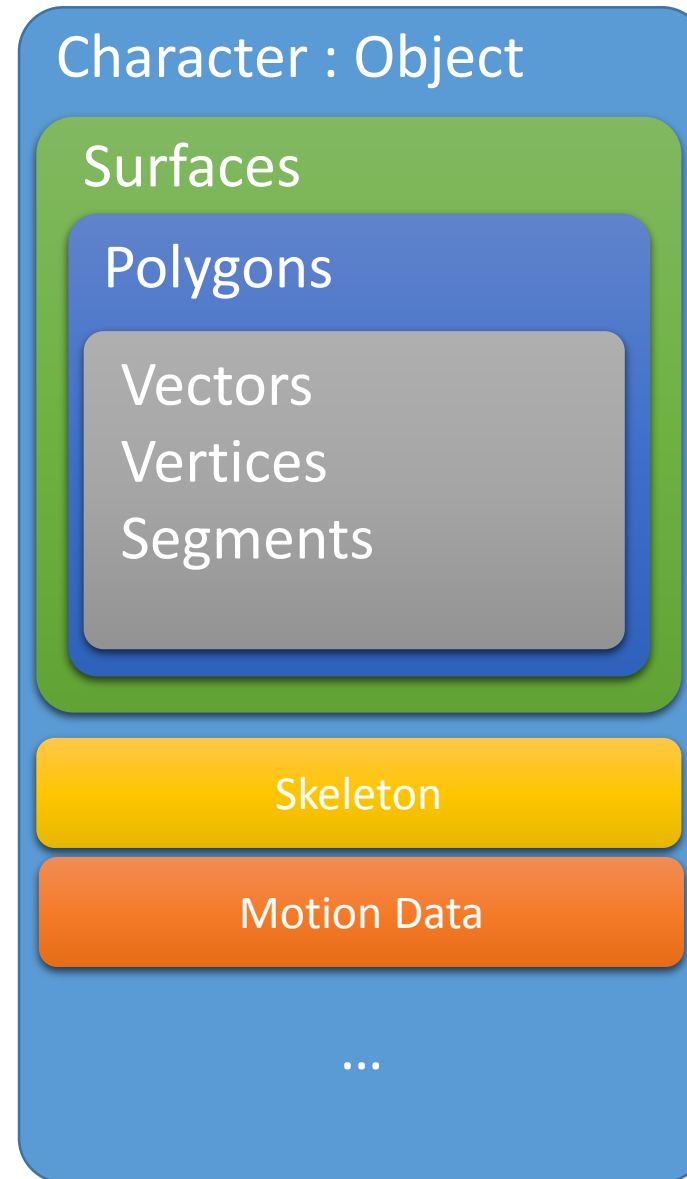
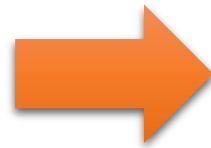
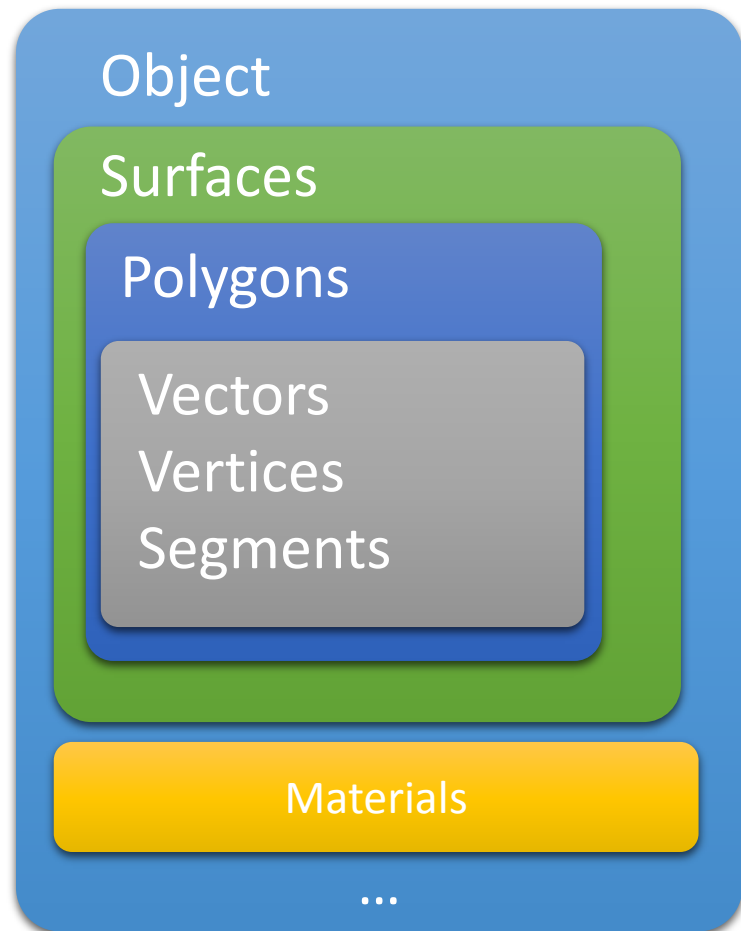




# Data Structures in a 3D Engine

- **Vertices/Vectors**
- Segments
- **Matrices**
- **Polygons**
- **Surfaces**
- **Materials**
- **Objects (Generic)**
- Super categories of Objects
- Lights
- Motion Data
- Lattices
- Skeletons
- Textures
- Particles
- ...

# Data Hierarchy





# Definition of a Vector Class

Class **TVector**

```
{
public:
    float x,y,z;
    TVector() {x=y=z=0;}
    void Clear();
    void vector(float xx,float yy,float zz);
    int operator == (TVector &v);
    int operator != (TVector &v);
    TVector operator - (TVector &v);
    TVector operator + (TVector &v);
    float operator * (TVector &v);
    TVector operator ^ (TVector &v);
    TVector operator / (TVector &v);
    TVector &operator -= (TVector &v);
    TVector &operator += (TVector &v);
    TVector &operator *= (TVector &v);
    TVector operator - (float &v);
    TVector operator + (float &v);
    TVector operator * (float &v);
    TVector operator / (float &v);
    TVector &operator -= (float &v);
    TVector &operator += (float &v);
    TVector &operator *= (float &v);
    TVector &operator /= (float &v);
    void Normalize();
    void Normalize(float MaxModule);
    float Module();
    void Scale(float s);
    void Reflect(TVector n);
    void Refract(TVector n, float RefIndex);
};
```

Initialization Methods  
Logic Operators

Vector - Vector Operators

Vector - Scalar Operators

Vector module operations

Reflection and Refraction

**typedef Vector Vertex;**



# Implementation Examples

```
int TVector::operator == (Vector &v)
{
    if(v.x==x && v.y==y && v.z==z) return 1;
    return 0;
}
```

```
TVector TVector::operator + (TVector &v)
{
    TVector t;
    t.x=v.x+x;
    t.y=v.y+y;
    t.z=v.z+z;
    return t;
}
```

```
float TVector::operator * (TVector &v)
{
    return v.x*x + v.y*y + v.z*z;
}
```

```
TVector TVector::operator ^ (TVector &v)
{
    TVector t;
    t.x=(y*v.z-z*v.y);
    t.y=(z*v.x-x*v.z);
    t.z=(x*v.y-y*v.x);
    return t;
}
```

```
void TVector::Normalize()
{
    float mod=(float)sqrt((float)x*x+y*y+z*z);
    if(mod!=0.0f)
    {
        mod = 1.0f/mod;
        x=(float)x*mod;
        y=(float)y*mod;
        z=(float)z*mod;
    }
}
```

```
void TVector::Reflect(TVector n)
{
    TVector t = * this;
    n.Scale(2.0f*(t*n));
    *this = t-n;
}
```

```
void TVector::Refract(TVector n,float RefIndex)
{
    n.Scale(-RefIndex);
    Vector t = *this;
    t.Scale(1.0f-RefIndex);
    *this = t+n;
}
```

Assignment: Build your own version of this library

# Normal calculation

```
TVertex v1,v2,v3;
```

```
TVector t,r,n;
```

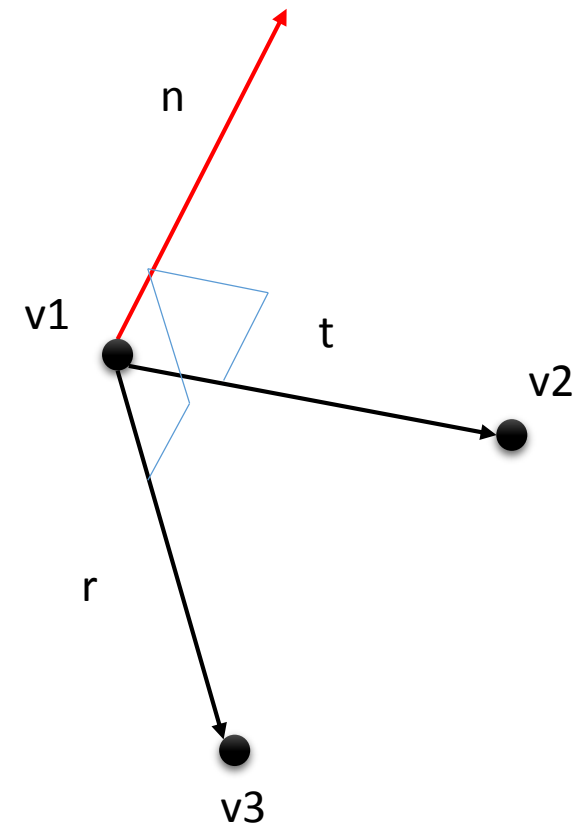
```
//initialization of v1,v2,v3 somewhere in the code
```

```
...
```

```
t = v2-v1;
```

```
r = v3-v1;
```

```
n = t^r;
```

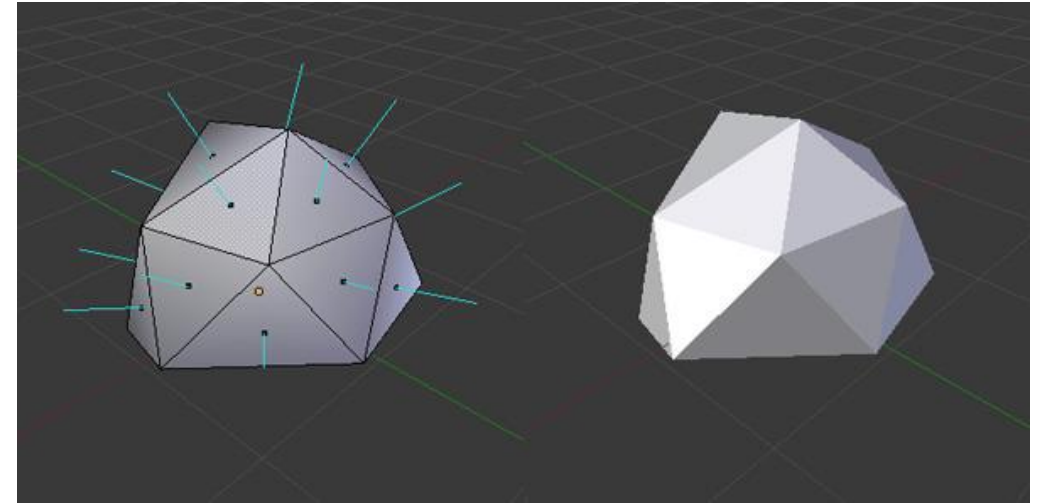


# Now we know how to calculate normals

```
for (i=0;i<PolyListLen;i++)  
{  
    TVector t,r,n;  
  
    t=Vlist[p[i].v2]-Vlist[p[i].v1];  
    r=Vlist[p[i].v3]-Vlist[p[i].v1];  
  
    p[i].Normal = t^r;  
    p[i].Normal.Normalize();  
}
```

//When I draw then...

```
glBegin(GL_TRIANGLES);  
    glNormal3f(p[i].n.x, p[i].n.y, p[i].n.z);  
    glVertex3f(Vlist[p[i].v1].x, Vlist[p[i].v1].y, Vlist[p[i].v1].z);  
    glVertex3f(Vlist[p[i].v2].x, Vlist[p[i].v2].y, Vlist[p[i].v2].z);  
    glVertex3f(Vlist[p[i].v3].x, Vlist[p[i].v3].y, Vlist[p[i].v3].z);  
glEnd();
```





# Definition of a Pose Class

```
Class TPose: TVector  
{  
  public:  
    float roll, pitch, yaw;  
    TPose() {x=y=z=roll=pitch=yaw=0;}  
};
```

Derived from the class TVector

Redefines the class constructor



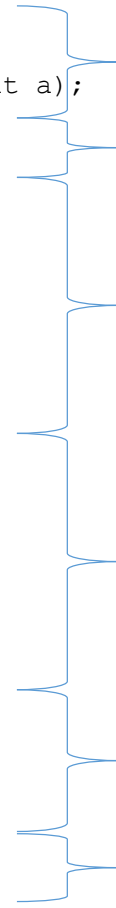
# Definition of a Color Class

Class **TColor**

```

{
public:
  float r,g,b,a;
  TColor() {r=g=b=a=0;}
  void Clear();
  void color(float r,float g,float b,float a);
  int operator == (Color &v);
  int operator != (TColor &v);
  TColor operator - (TColor &v);
  TColor operator + (TColor &v);
  float operator * (TColor &v);
  TColor operator ^ (TColor &v);
  TColor operator / (TColor &v);
  TColor &operator -= (TColor &v);
  TColor &operator += (TColor &v);
  TColor &operator *= (TColor &v);
  TColor operator - (float &v);
  TColor operator + (float &v);
  TColor operator * (float &v);
  TColor operator / (float &v);
  TColor &operator -= (float &v);
  TColor &operator += (float &v);
  TColor &operator *= (float &v);
  TColor &operator /= (float &v);
  void Normalize();
  void Normalize(float MaxModule);
  float Module();
  void Scale(float s);
};

```



Initialization Methods  
Logic Operators

Vectorial Operators

Vector - Scalar Operators

Vector module operations

Reflection and Refraction





# Definition of a Matrix 4x4 Class

```
class TMatrix4x4
{
public:
    float m[16];

    TMatrix4x4() {Clear();}
    void Clear();
    void LoadIdentity();
    void Transpose();
    void Invert();
    void Mul(TMatrix4x4 * M);
    void Scalar(float s);
    float Determinant();
    ...
    Vector operator * (Vector &v);
};
```

```
void TMatrix4x4::LoadIdentity()
{
    m[ 1]=m[ 2]=m[ 3]=m[ 4]=
    m[ 6]=m[ 7]=m[ 8]=m[ 9]=
    m[11]=m[12]=m[13]=m[14]=0.0f;
    m[ 0]=m[ 5]=m[10]=m[15]=1.0f;
}
```

```
void TMatrix4x4::Transpose()
{
    float a;
    a=m[ 1]; m[ 1]=m[ 4]; m[ 4]=a;
    a=m[ 2]; m[ 2]=m[ 8]; m[ 8]=a;
    a=m[ 3]; m[ 3]=m[12]; m[12]=a;
    a=m[ 6]; m[ 6]=m[ 9]; m[ 9]=a;
    a=m[ 7]; m[ 7]=m[13]; m[13]=a;
    a=m[11]; m[11]=m[14]; m[14]=a;
}
```

```
void TMatrix4x4::Clear()
{
    m[ 0]=m[ 1]=m[ 2]=m[ 3]=
    m[ 4]=m[ 5]=m[ 6]=m[ 7]=
    m[ 8]=m[ 9]=m[10]=m[11]=
    m[12]=m[13]=m[14]=m[15]=0.0f;
}
```

```
void TMatrix4x4::Mul(TMatrix4x4 * M)
{
    TMatrix4x4 r;
    r.m[ 0] = m[ 0]*M->m[ 0] + m[ 1]*M->m[ 4] + m[ 2]*M->m[ 8] + m[ 3]*M->m[12];
    r.m[ 1] = m[ 0]*M->m[ 1] + m[ 1]*M->m[ 5] + m[ 2]*M->m[ 9] + m[ 3]*M->m[13];
    r.m[ 2] = m[ 0]*M->m[ 2] + m[ 1]*M->m[ 6] + m[ 2]*M->m[10] + m[ 3]*M->m[14];
    r.m[ 3] = m[ 0]*M->m[ 3] + m[ 1]*M->m[ 7] + m[ 2]*M->m[11] + m[ 3]*M->m[15];

    r.m[ 4] = m[ 4]*M->m[ 0] + m[ 5]*M->m[ 4] + m[ 6]*M->m[ 8] + m[ 7]*M->m[12];
    r.m[ 5] = m[ 4]*M->m[ 1] + m[ 5]*M->m[ 5] + m[ 6]*M->m[ 9] + m[ 7]*M->m[13];
    r.m[ 6] = m[ 4]*M->m[ 2] + m[ 5]*M->m[ 6] + m[ 6]*M->m[10] + m[ 7]*M->m[14];
    r.m[ 7] = m[ 4]*M->m[ 3] + m[ 5]*M->m[ 7] + m[ 6]*M->m[11] + m[ 7]*M->m[15];

    r.m[ 8] = m[ 8]*M->m[ 0] + m[ 9]*M->m[ 4] + m[10]*M->m[ 8] + m[11]*M->m[12];
    r.m[ 9] = m[ 8]*M->m[ 1] + m[ 9]*M->m[ 5] + m[10]*M->m[ 9] + m[11]*M->m[13];
    r.m[10] = m[ 8]*M->m[ 2] + m[ 9]*M->m[ 6] + m[10]*M->m[10] + m[11]*M->m[14];
    r.m[11] = m[ 8]*M->m[ 3] + m[ 9]*M->m[ 7] + m[10]*M->m[11] + m[11]*M->m[15];

    r.m[12] = m[12]*M->m[ 0] + m[13]*M->m[ 4] + m[14]*M->m[ 8] + m[15]*M->m[12];
    r.m[13] = m[12]*M->m[ 1] + m[13]*M->m[ 5] + m[14]*M->m[ 9] + m[15]*M->m[13];
    r.m[14] = m[12]*M->m[ 2] + m[13]*M->m[ 6] + m[14]*M->m[10] + m[15]*M->m[14];
    r.m[15] = m[12]*M->m[ 3] + m[13]*M->m[ 7] + m[14]*M->m[11] + m[15]*M->m[15];
    *this = r;
}
```

Assignment: Build your own version of this library



# Polygon Class

```
class TPolygon
{
public:
    int    v1,v2,v3;    //indices to the 3 vertices
    int    Visible;    //visibility flag
    TVector Normal;    //Normal vector
    TColor Color;      //color
    void    CalcNormal (); //calculate Normal
    void    Flip ();    //flip the normal orientation
    void    Draw ();    //draw
};
```

```
void TPolygon::CalcNormal()
{
    Vector t,r,n;
    t = Vlist[v2]-Vlist[v1];
    r = Vlist[v3]-Vlist[v1];
    Normal = t^r;
    Normal.Normalize();
}
```

```
void TPolygon::Flip()
{
    int a = v2;
    v2 = v3;
    v3 = v2;
    CalcNormal();
}
```

```
void TPolygon::Draw()
{
    if(Visible)
    {
        glBegin(GL_TRIANGLES);
        glNormal3f(Normal.x, Normal.y, Normal.z);
        glVertex3f(Vlist[v1].x, Vlist[v1].y, Vlist[v1].z);
        glVertex3f(Vlist[v2].x, Vlist[v2].y, Vlist[v2].z);
        glVertex3f(Vlist[v3].x, Vlist[v3].y, Vlist[v3].z);
        glEnd();
    }
}
```

For example... NB: This model doesn't consider the vertex optimization



# Surface Class

```
class TSurface
{
public:
    TVertex      VList[...];    //Vertices on the surface
    unsigned int VListLen;     //Number of Vertices
    TPolygon     Plist[...];    //Polygons on the surface
    unsigned int PListLen;     //Number of Polygons on the surface
    TColor       Color;        //Surface color
    int          Visible;      //Visibility Flag
    void         CalcNormals(); //calculate Normal
    void         Flip();       //flip the normal orientation
    void         Draw();       //draw
};
```

```
void TSurface::CalcNormal()
{
    int i;
    for(i=0;i<PListLen;i++)
        Plist[i].CalcNormal();
}
```

```
void TSurface::Flip()
{
    int i;
    for(i=0;i<PListLen;i++)
        Plist[i].Flip();
}
```

```
void TSurface::Draw()
{
    if(Visible)
    {
        int i;
        glColor4f(Color.r,Color.g,Color.b,Color.a);
        for(i=0;i<PListLen;i++)
            Plist[i].Draw();
    }
}
```

For example... NB: This model doesn't consider the vertex optimization



# Object Class

```
class TObject
{
public:
    TPose          Pose;          //Object Pose
    Tvector        Scale;        //Object Scale
    TMatrix4x4     TRS;          //Model View Matrix
    TSurface       SList[...];    //Surfaces of the Object
    unsigned int   SListLen;     //Number of Surfaces
    int            Visible;      //Visibility Flag
    void           CalcNormals(); //calculate Normal
    void           BuildjMatrix(); //Builds the TRS Matrix
    void           Draw();       //draw
};
```

```
void TObject::CalcNormal()
{
    int i;
    for(i=0;i<SListLen;i++)
        Slist[i].CalcNormal();
}
```

```
void TObject::Draw()
{
    if(Visible)
    {
        int i;
        for(i=0;i<SListLen;i++)
            Slist[i].Draw();
    }
}
```

```
void TObject:: BuildMatrix()
{
    glLoadIdentity(); // loads the identity matrix
    glTranslatef(Pose.x, Pose.y, Pose.z); // translate the object to the desired position
    glRotatef(Pose.yaw, 0.0f, 1.0f, 0.0f); // rotation around Y axis
    glRotatef(Pose.pitch, 1.0f, 0.0f, 0.0f); // rotation around X axis
    glRotatef(Pose.roll, 0.0f, 0.0f, 1.0f); // rotation around Z axis
    glScalef(Scale.x, Scale.y, Scale.z); // Scale object
    glGetFloatv(GL_MODELVIEW_MATRIX, TRS);
}
```

For example... NB: This model doesn't consider the vertex optimization



# Camera Class

```
class TCamera
{
public:
    TPose          POV;          //Object Pose
    TMatrix4x4    TR;           //TR Matrix
    void          BuildMatrix(); //Builds the TRS Matrix
};
```

```
void TObjct:: BuildMatrix()
{
    glMatrixMode(GL_MODELVIEW); // select the modelview mode transformation of the entities
    glLoadIdentity();           // loads the identity matrix
    glRotatef   (-POV.yaw  ,0.0f,1.0f,0.0f); // rotation around Y axis
    glRotatef   (-POV.pitch,1.0f,0.0f,0.0f); // rotation around X axis
    glRotatef   (-POV.roll ,0.0f,0.0f,1.0f); // rotation around Z axis
    glTranslatef(-POV.tx,-POV.ty,POV.tz);   // translate the camera to the desired position
    glGetFloatv( GL_MODELVIEW_MATRIX , TR);
}
```

For example... NB: This model doesn't consider the vertex optimization



# Scene Class

```
class TScene
{
public:
    Tcamera      Camera;
    Tobject      OList [...];           //List of objects
    unsigned int OListLen;             //Number of objects
    int          Visible;              //Visibility Flag
    void         InitScene ();         //Initialize Scene Geometry
    void         BuildSceneMatrices (); //builds the scene matrices
    void         Draw ();              //draw scene
};
```

```
void TScene::InitScene()
{
    int i;
    for(i=0;i<OListLen;i++)
        Slist[i].CalcNormal();
}
```

```
void TScene:: BuildSceneMatrices()
{
    Camera.BuildMatrix()
    int i;
    for(i=0;i<OListLen;i++)
        OList[i].BuildMatrix();
}
```

```
void TScene::Draw()
{
    if(Visible)
    {
        int i;
        for(i=0;i<OListLen;i++)
        {
            glLoadMatrixf(Camera.TR); //Load the Camera Matrix
            glMultMatrixf(OList[i].TRS); //Multiplies for the Obj Matrix
            OList[i].Draw();
        }
    }
}
```

For example... NB: This model doesn't consider the vertex optimization



# EngineVR Class

```
class TEngineVR
{
public:
    Tscene          SCList[...];    //Available Scenes
    unsigned int    SCListLen;      //Number of Scenes
    unsigned int    CurrentScene;  //Selected Scene
    void            InitScene();  //Initializes selected Scene
    void            RenderScene(); //draw scene
};
```

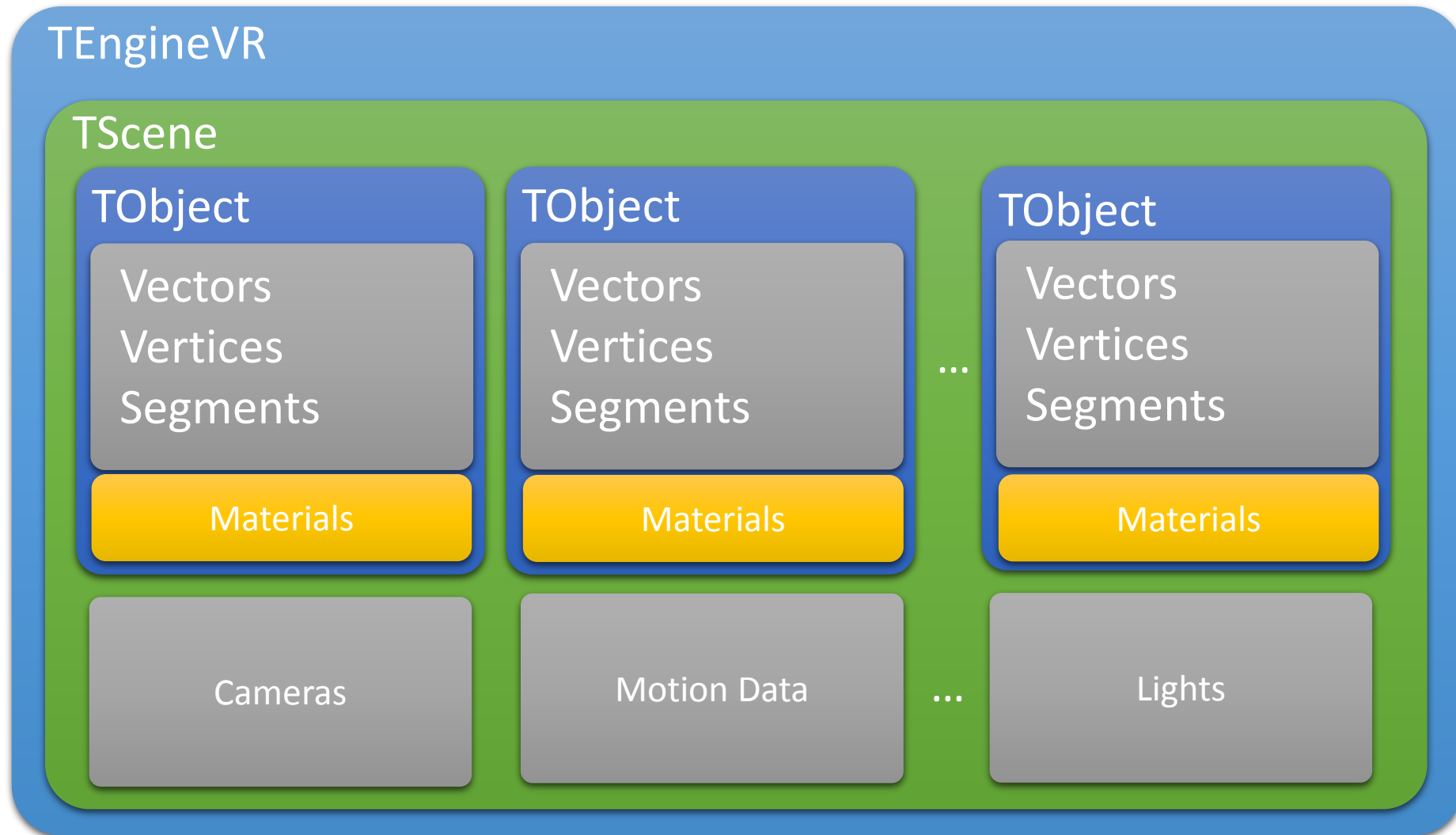
```
void TEngineVR::InitScene()
{
    SCList[CurrentScene].CalcNormal();
}
```

```
void TEngineVR::RenderScene()
{
    SCList[CurrentScene].Draw();
}
```

For example... NB: This model doesn't consider the vertex optimization



# Data Structure







# Data Structures in a 3D Engine

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- **Polygons**
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- Particles
- ...